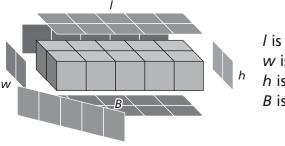


Dear Family,

In this unit, we are reviewing the volume of rectangular prisms with whole number edge lengths, and analyzing the difference between surface area and volume along with the units used to measure them.

The **surface area** of a solid figure is the total area of all its faces. **Volume** is the measure of the space that a three-dimensional figure occupies. The solid figure below is made of centimeter cubes.



I is the length. *w* is the width. *h* is the height. *B* is the area of the base.

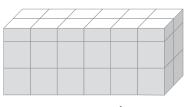
Surface Area $SA = (2 \times 10) + (2 \times 2) + (2 \times 5) = 34$

Surface Area = 34 cm^2

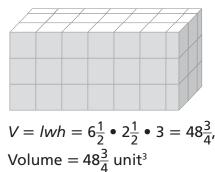
Volume V = lwh or V = Bh $V = 5 \times 2 \times 1$ or $V = 10 \times 1$ Volume = 10 cm³

Surface area is measured in **square units**. Volume is measured in **cubic units**.

This unit also introduces the volume of rectangular prisms with fractional edge lengths.



 $V = Bh = 12 \cdot 2\frac{1}{2} = 30$, Volume = 30 unit³



If you need practice materials or if you have any questions, please call or write to me.

Sincerely, Your child's teacher



Unit 6 addresses the following standards from the *Common Core State Standards for Mathematics with California Additions*: 6.G.1, 6.G.2, 6.G.4, 6.EE.2, 6.EE.2c, and all Mathematical Practices.

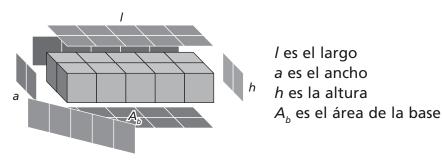


Un vistazo general al contenido

Estimada familia:

En esta unidad, repasaremos cómo obtener el volumen de prismas rectangulares cuyos lados tienen longitudes expresadas en números enteros. También analizaremos la diferencia entre el área total y el volumen y examinaremos las unidades de medida usadas.

El **área total** de un cuerpo geométrico es la suma del área de todas sus caras. El **volumen** es la medida del espacio que ocupa una figura tridimensional.

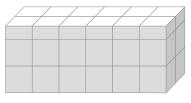


Área total

 $A_t = (2 \times 10) + (2 \times 2) +$ (2 × 5) = 34 Área total = 34 cm² Volumen $V = lah \circ V = A_b h$ $V = 5 \times 2 \times 1 \circ V = 10 \times 1$ Volumen = 10 cm³

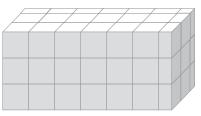
El área total se mide en **unidades cuadradas**. El volumen se mide en **unidades cúbicas**.

En esta unidad también se presenta el volumen de prismas rectangulares cuyos lados tienen longitudes expresadas en fracciones.



 $V = A_{b}h = 12 \cdot 2\frac{1}{2} = 30,$

Volumen = 30 unidades^3



 $V = lah = 6\frac{1}{2} \cdot 2\frac{1}{2} \cdot 3 = 48\frac{3}{4}$ Volumen = $48\frac{3}{4}$ unidades³

Si necesita material para practicar o si tiene preguntas, por favor comuníquese conmigo.

Atentamente, El maestro de su hijo

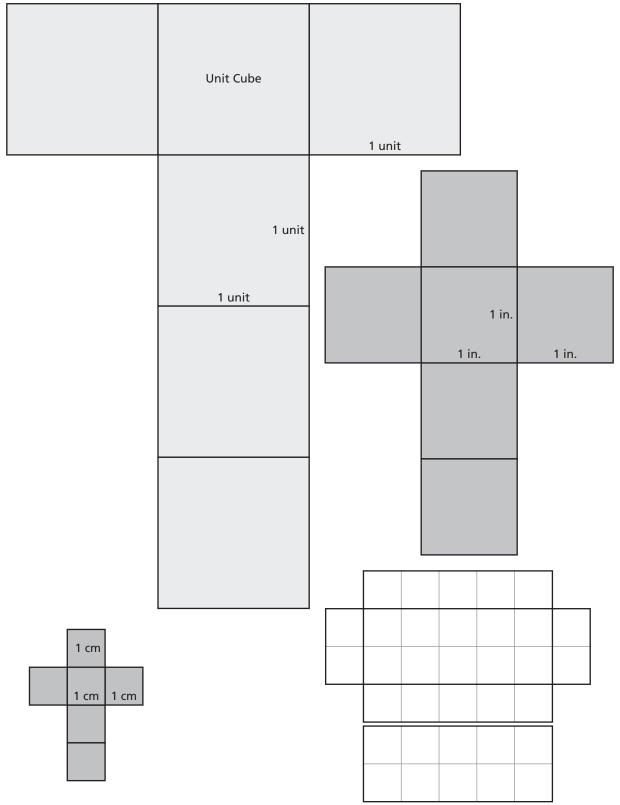


En la Unidad 6 se aplican los siguientes estándares auxiliares, contenidos en los Estándares estatales comunes de matemáticas con adiciones para California: 6.G.1, 6.G.2, 6.G.4, 6.EE.2, 6.EE.2c, y todos los de prácticas matemáticas.



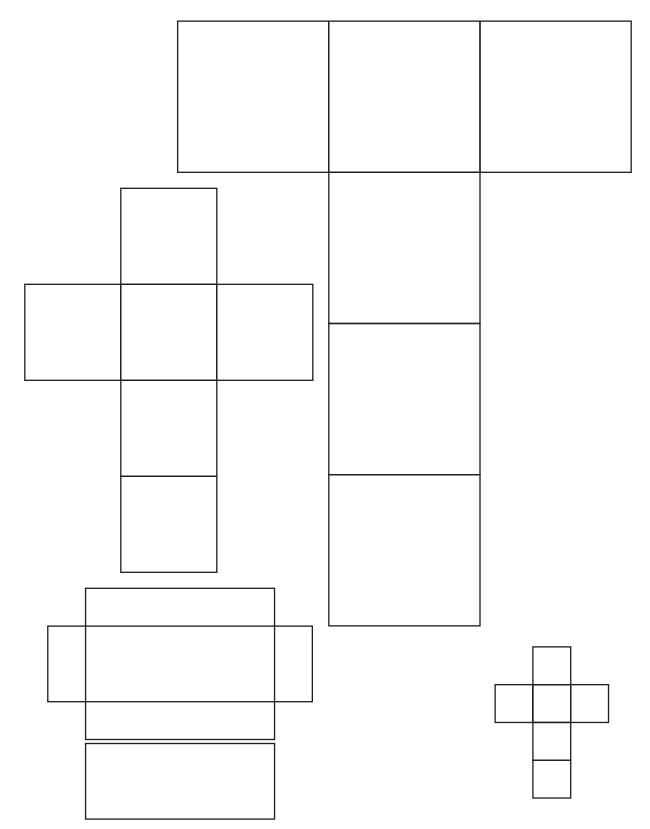
► Nets for Cubic Units and a Rectangular Prism

Cut out the nets and form the solid figure.





► Nets for Cubic Units and a Rectangular Prism (continued)





CACC Content Standards 6.G.1, 6.G.4, 6.EE.2, 6.EE.2c Mathematical Practices MP.3, MP.6, MP.7

► Cubic Units

The volume of a solid figure is the amount of space occupied by the figure. Volume is measured in cubic units.



 How can you measure the amount of space each of these rectangular prisms takes up? How much space is inside each of the rectangular prisms? How many unit cubes does it take to fill the rectangular prism?

A **unit cube** is a cube with each edge 1 unit long. The volume of a unit cube is 1 cubic unit. It can be written 1 cubic unit or 1 unit³.

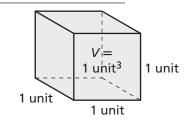
2. Label the length, width, and height of the centimeter cube on the right. Write the volume of a centimeter cube in two ways.

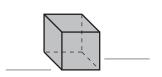
Write the volume of the cube in two ways.

 3. inch cube
 4. meter cube
 5. foot cube
 6. yard cube

Vocabulary

volume unit cube centimeter cube inch cube cubic unit (unit³) cubic centimeter (cm³) cubic inch (in.³)



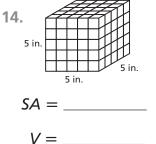




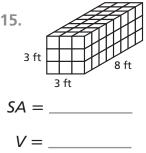
► How Are Surface Area and Volume Different?

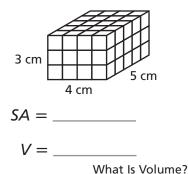
Complete.

7. What is the surface area of the unit cube you made? 8. What is the surface area of an inch cube? 9. How is volume different than surface area? 10. How is the unit used to measure surface area different from the unit used to measure volume? 11. What is the surface area and volume of the prism you made? SA = _____ V =12. Write a formula for the surface area of the prism. SA = _____ 13. Write two formulas for the volume of a rectangular prism. V = V =Find the surface area and volume of the prisms. 15. 16.



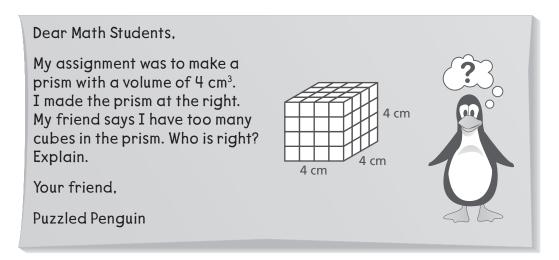
260 UNIT 6 LESSON 1







► What's the Error?



17. Write a response to the Puzzled Penguin.

h Students, he volume of a cube cm by 2 cm by 2 cm to be t when I built the cube ntimeter cubes it took and not 6. What did ng? nd, Penguin

18. Write a response to the Puzzled Penguin.



► Choose a Measure

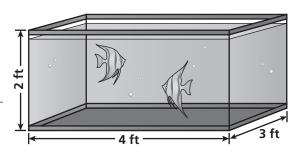
Choose the most appropriate measure. Write *perimeter*, *surface area*, or *volume*.

- 19. the distance around a building _____
- 20. the amount of wrapping paper on a gift box _____
- 21. the amount of sand in a sand box _____
- 22. the amount of wall space in a room _____
- 23. the length of a fence around a yard ______
- 24. the amount of peanuts in a container _____

► Solve Real World Problems

Solve.

- 25. How many cubic feet of water will it take to fill this aquarium? What is the open surface area of the water?
- 26. Hal wants to make a hole in the wall of his restaurant to display one of the larger faces of this aquarium. He cut a hole that is 25 in. high by 27 in. long. Will the aquarium fit? Explain.

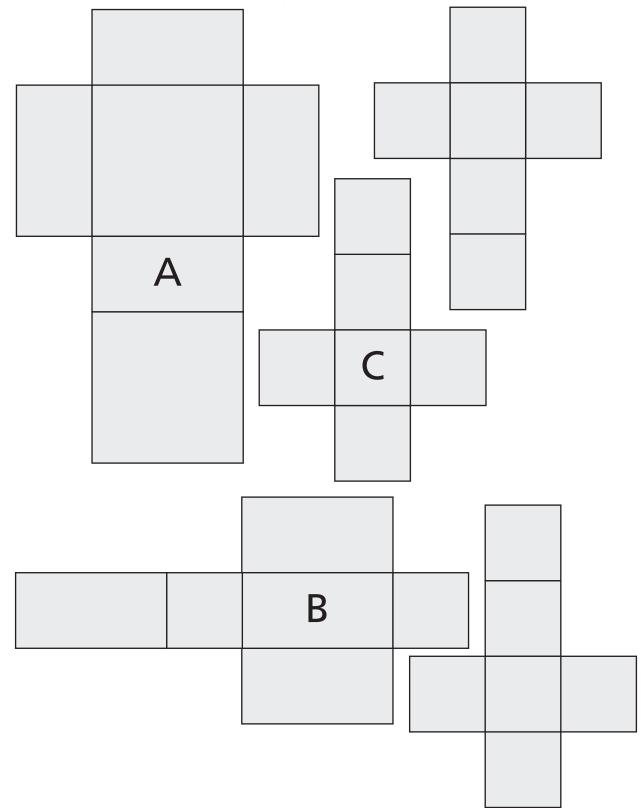


- 27. The sides of this aquarium are glass. How much glass did it take to make the aquarium?
- 28. What is the greatest number of rectangular 2 in.
 × 2 in. × 4 in. boxes that will fit in a carton with a volume of 3,456 in.³ and a 12 in. × 24 in. rectangular base?

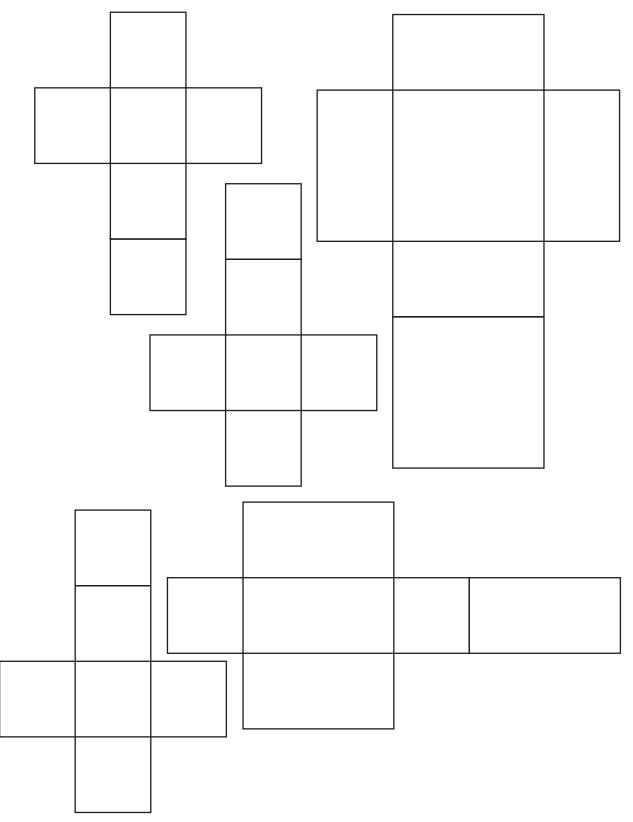


► Nets for Part of a Unit Cube

Cut out the nets and form the solid figures.



► Nets for Part of a Unit Cube (continued)





Rectangular Prisms with Volumes Less Than 1 Cubic Unit

Place the cubes on your desk in order from greatest volume to least volume as shown below.

Unit Cube	Prism A	Prism B	Prism C
1 cubic unit	$\frac{1}{2}$ cubic unit		
	2	of Prism A	of Prism B
1. How many of each make the Unit Cube	of these prisms does it e?	take to	
Prism A:	Prism B:	Prism C:	
2. What is the volume	of each prism?		
Prism A	Prism B	Prism C	
V =	V =	V =	

Some students found the volume of prism B by multiplying.

	Volume of Prism B	Volume of Prism C
Terence	$\frac{1}{2}$ of $\frac{1}{2}$ of a unit cube or $\frac{1}{4}$ unit ³ .	
Serena	$\frac{1}{2} \cdot \frac{1}{2}$ of a cubic unit or $\frac{1}{4}$ unit ³ .	
Emma	It takes $\frac{1}{4}$ of a unit cube or $\frac{1}{4}$ unit ³ to make prism B.	

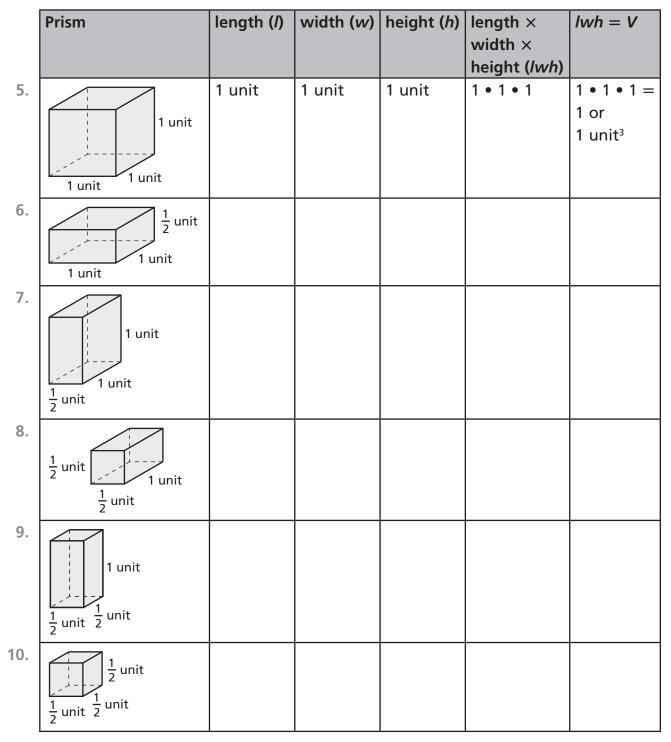
3. Why are all 3 descriptions correct?

4. Complete the chart to show how Terrence, Serena, and Emma would describe the volume of Prism C.



► Calculate Volume Less Than 1 Cubic Unit

Complete the table.

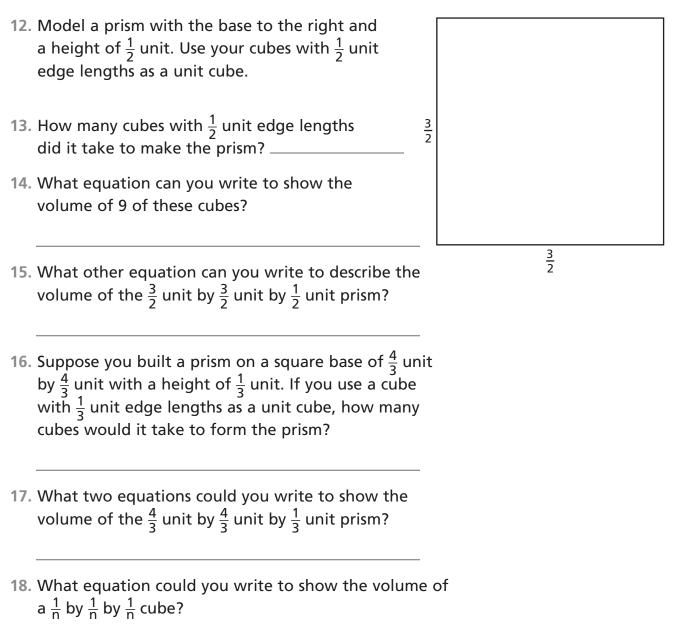


11. How is the volume of a prism related to the length, width, and height of the prism?



► Find Volume by Packing with Unit Cubes

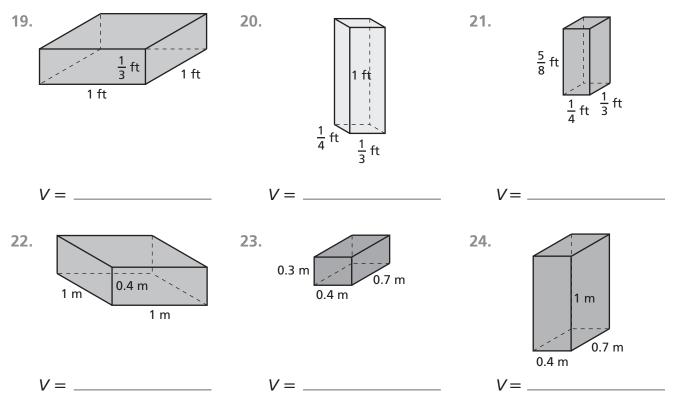
Solve.





Volumes of Prisms with Fractional Edge Lengths

Find the volume.

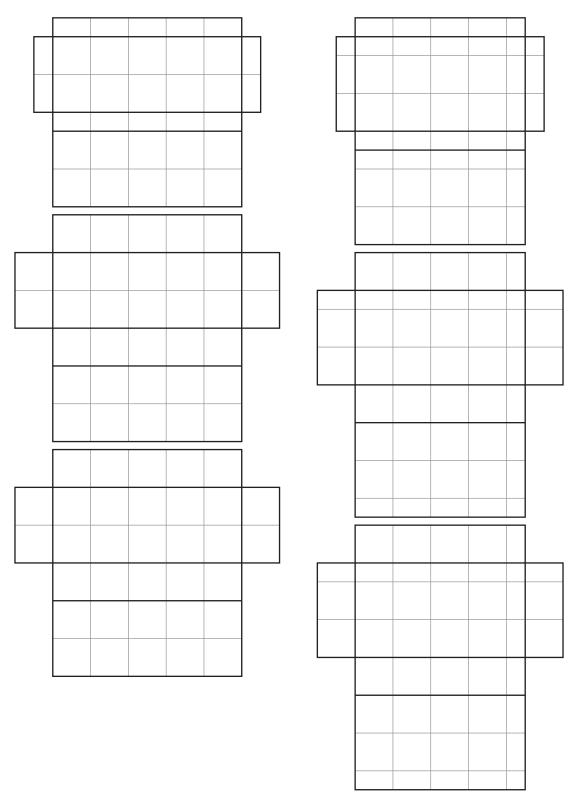


- 25. Describe two different rectangular prisms that each have a volume of $\frac{6}{175}$ in.³
 - a. What three factors will result in a product of 6?
 - c. What fractions can you make with these factors that could be the dimensions of one rectangular prism?
- b. What three factors will result in a product of 175?
- d. What different fractions can you make with these factors that could be the dimensions of a different rectangular prism?
- **26.** Describe two different rectangular prisms that each have a volume of 0.125 m³.

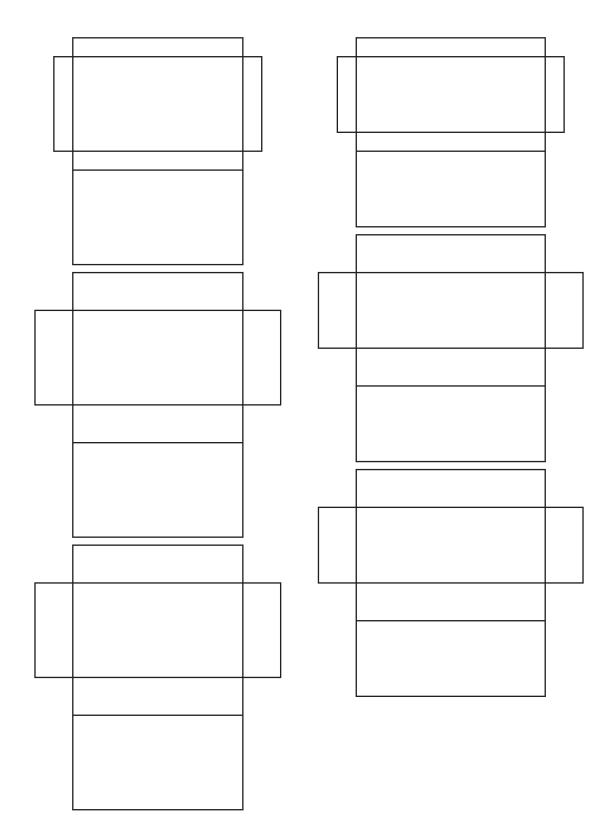


► Prism Layers

Cut out the nets and form the solid figures.



► Prism Layers (continued)

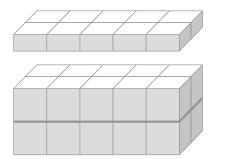




CACC Content Standards 6.G.1, 6.G.2, 6.EE.2, 6.EE.2c Mathematical Practices MP.1, MP.3, MP.6

• Build a Prism with Whole and Half Layers

Here is how to build a prism that has a length of 5 cm, a width of 2 cm, and a height of $2\frac{1}{2}$ cm using whole and half layers.



- Stack two layers of a prism that has a 5 cm by 2 cm base and is 1 cm tall.
- Next stack one layer of a prism that has a 5 cm by 2 cm base and is ¹/₂ cm tall.

Build prisms with whole and half layers to complete the table below.

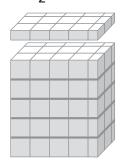
	length (/) (in cm)	width (<i>w</i>) (in cm)	length × width (<i>lw</i>)	Area of Base (<i>B</i>)		V = Bh
1.	5	2	5•2	10 10 cm ²	$\frac{1}{2}$ cm	
2.	5	2			1 cm	
3.	5	2			$1\frac{1}{2}$ cm	
4.	5	2			2 cm	
5.	5	2			$3\frac{1}{2}$ cm	
6.	5	2			4 cm	
7.	5	2			$4\frac{1}{2}$ cm	
8.	5	2			5 cm	
9.	5	2			$5\frac{1}{2}$ cm	

10. Explain the expression you wrote for the volume of the prism with the $3\frac{1}{2}$ cm height in terms of layers of cubes.



• Build a Prism with Fractional Base Dimensions

Here is how to build a prism that has a length of $4\frac{1}{2}$ cm and a width of $2\frac{1}{2}$ cm and a height of $5\frac{1}{2}$ cm using whole and half layers.



- Stack five layers of a prism that has a $4\frac{1}{2}$ cm by $2\frac{1}{2}$ cm base and is 1 cm tall.
- Next stack one layer of a prism that has a $4\frac{1}{2}$ cm by $2\frac{1}{2}$ cm base and is $\frac{1}{2}$ cm tall.

Use this table to record the volumes of the prisms you build.

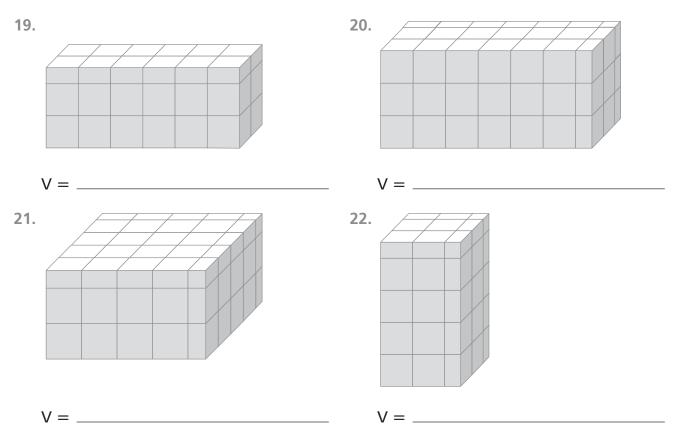
	length (/) (in cm)	width (<i>w</i>) (in cm)	Area of Base (B)	height (<i>h</i>)	V = Bh
11.	4 <u>1</u> 2	$2\frac{1}{2}$	$11\frac{1}{4}$ $11\frac{1}{4}$ cm ²	1cm	$V = 11\frac{1}{4} \bullet 1 = 11\frac{1}{4}$ $V = 11\frac{1}{4} \text{ cm}^3$
12.	$4\frac{1}{2}$	$2\frac{1}{2}$		$\frac{1}{2}$ cm	
13.	$4\frac{1}{2}$	$2\frac{1}{2}$		$1\frac{1}{2}$ cm	
14.	4 <u>1</u>	2 <u>1</u>		$2\frac{1}{2}$ cm	
15.	4 <u>1</u>	2 <u>1</u> 2		$3\frac{1}{2}$ cm	
16.	4 <u>1</u>	2 <u>1</u>		4 cm	
17.	$4\frac{1}{2}$	$2\frac{1}{2}$		$4\frac{1}{2}$ cm	

18. Explain the expression you wrote for the volume of the prism with a $2\frac{1}{2}$ cm height in terms of layers of cubes.



► Use Formulas

Find the volume. Each cube represents 1 cm³.



23. Explain why we can use the two formulas below for the volume of a prism. V stands for the volume of the rectangular prism. I and w stand for the length and width of the base, h stands for the height, and B stands for the area of the base.

V = lwh

V = Bh



Find the Unknown Dimension or Volume

Show your work

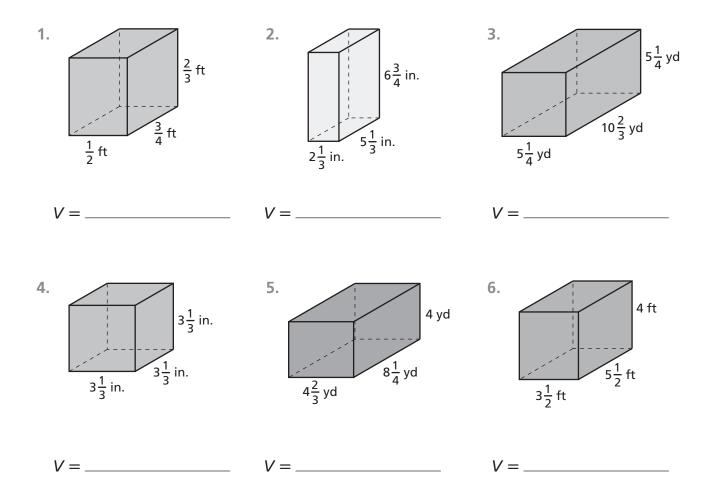
Write and solve an equation.

- 24. A ring box in the shape of a rectangular prism has a volume of 25 cm³ and is $2\frac{1}{2}$ cm tall. What is the area of the base (B) of the ring box?
- **25.** A jewelry box in the shape of a rectangular prism has a volume of 90 in.³ and a height of $2\frac{1}{2}$ in. What are possible whole dimensions for the length and width of the base?
- **26.** A storage tank in the shape of a rectangular prism has a volume of 35 m³ and a height of 2.5 m. The length of the base of the prism is 3.5 m. What is the width of the base of the storage tank?
- 27. A shipping box in the shape of a rectangular prism has a volume of $1\frac{1}{2}$ ft³. The area of the base is $\frac{2}{3}$ ft². What is the height of the shipping box?
- 28. A small trunk in the shape of a rectangular prism has a volume of 0.15 m³. The area of the base is 0.25 m². What is the height of the small trunk?
- **29.** A stack of sticky notes in the shape of a rectangular prism has a base with an area of $1\frac{1}{8}$ in.² and a height that is $1\frac{1}{3}$ in. What is the volume of the stack of sticky notes?
- 30. An eraser in the shape of a rectangular prism has a length of 3.5 cm, a width of 2.8 cm and a height 1.4 cm. What is the volume of the eraser?



► Volumes of Prisms with Fractional Edge Lengths

Write a numerical expression for the volume. Then calculate the volume.



Find the unknown dimension or volume of each rectangular prism.

7. <i>l</i> = 4.5 cm	8. $V = 156 \text{ ft}^3$	9. $V = 209.3 \text{ m}^3$	10. <i>V</i> = 279 in. ³
<i>w</i> = 2.7 cm	$l = 4\frac{4}{5}$ ft	<i>l</i> = 7 m	$w = 6\frac{1}{5}$ in.
<i>h</i> = 3.2 cm	$w = 6\frac{1}{2}$ ft	<i>h</i> = 4.6 m	$h = 7\frac{1}{2}$ in.
V =	h =	w =	/ =



► Solve Real World Problems

Show your work

Solve.

- 11. A 20 ft by 20 ft square garden is being covered with3 in. of mulch. How many cubic feet of mulch will be needed?
- 12. A rectangular cargo container is 2.5 m wide, 3.1 m tall, and 10 m long. What is the volume of the container in cubic meters?
- **13.** Sue's collection of baseball cards forms a stack that is 3 in. high. If the cards are $2\frac{1}{4}$ in. wide and $5\frac{1}{2}$ in. long. What is the volume of the stack of cards?
- 14. Sue bought a box to hold her baseball cards. The box is $2\frac{1}{2}$ in. wide and $5\frac{1}{2}$ in. long and has a volume of 55 in.³ How tall a stack of cards can fit in the box?
- 15. A rectangular shipping box has a bottom that is 1 ft by 2 ft. The height of the box is 9 in. What is the volume of the box in cubic feet?
- 16. A tree ornament comes in a box that is $5\frac{1}{2}$ in. tall with a square top and bottom. The box has a volume of $49\frac{1}{2}$ in.³ How long is each side of the base?
- **17.** A foam mattress measures $3\frac{1}{3}$ ft by $6\frac{2}{3}$ ft by 6 in. How many cubic feet of foam form the mattress?



CACC Content Standards 6.G.1, 6.G.2, 6.G.4, 6.EE.2, 6.EE.2c Mathematical Practices MP.1, MP.3, MP.6

► Units for *I*, *w*, *h*, *B*, and *V*

If V is the volume of the prism, then we can write these formulas.

V = lwh V = Bh

These equations show how the volume of the prism is related to other dimensions of the prism.

Complete.

1. If the value for h is given in centimeters , what unit

should we use for I and w?

2. If the values for *I*, *w*, and *h* are given in centimeters,

what unit should we use for B? _____

3. If the values for *I*, *w*, and *h* are given in centimeters,

what unit should we use for V? _____

► What's the Error?

Dear Math Students,

Here is how I found the number of cubic feet of mulch needed on the garden pictured at the right.

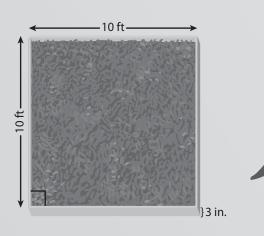
V = Iwh

 $V = 10 \cdot 10 \cdot 3 = 300$

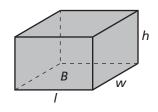
The volume is 300 ft³.

My friend says this is not the correct answer. What did I do wrong?

Your friend, Puzzled Penguin



4. Write a response to the Puzzled Penguin.





► What's the Error?

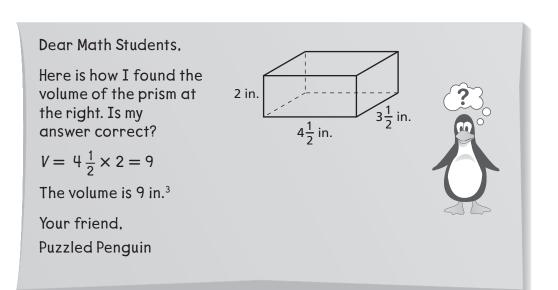
Dear Math Students,

I see in the formula V = lwh that I need to multiply three edge lengths to find the volume. The prism has a lot more edges. Why don't we multiply all the edge lengths to find the volume?

Your friend,

Puzzled Penguin

5. Write a response to the Puzzled Penguin.

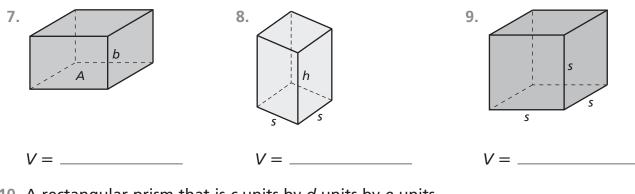


6. Write a response to the Puzzled Penguin.



► Write Equations for Volume

Write an equation for volume, V, using the variables given.



10. A rectangular prism that is c units by d units by e units has a volume, V, cubic units. Write an equation relating

c, d, e, and V. _____

- 11. A rectangular prism has a base area of *M* square units and is *t* units tall. Write an equation relating *M*, *t*, and *V*.
- A rectangular prism is 5 units tall and has a base area of W square units. Write an equation relating W and V.

► Surface Area and Volume of a Cube

Solve.

Each edge of a cube is $\frac{1}{2}$ in. long.		
13. What is the surface area of the cube?	14.	What is the volume of the cube?
A cube has a volume of 8 m ³ .		
15. What is the length of each edge?	16.	What is the surface area of the cube?
One face of a cube has an area of 2.25 cm ² .		
17. What is the length of each edge?	18.	What is the volume of the cube?



► Solve Real World Problems

Solve.

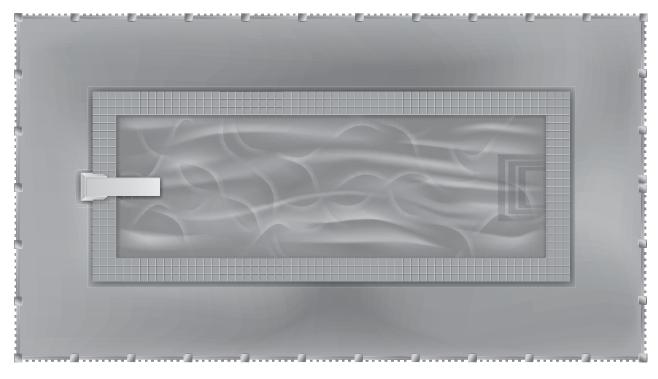
Show your work

- **19.** An aquarium is 18 in. by 16 in. by 12 in. Water fills $\frac{3}{4}$ of the aquarium. What is the volume of the water?
- **20.** A sandbox is 5 ft by 6 ft by 1 ft. Sand fills half the sandbox. What is the volume of the sand?
- 21. Which holds more: two cube containers with $12\frac{1}{2}$ ft edges or one rectangular prism container with height $12\frac{1}{2}$ ft, width 11 ft, and length 25 ft? How much more?
- 22. Which has the greatest surface area: A cube gift box with $\frac{1}{2}$ ft edges or a rectangular prism gift box with a height of $\frac{1}{2}$ ft, width $\frac{1}{4}$ ft, and length 1 ft? How much more?
- 23. The length of a shipping box is twice its width. The width of the box is $7\frac{1}{2}$ in. The height is $2\frac{1}{2}$ in. less than the length. What is the volume of the box?
- 24. If a mailbox at a post office rents for one year for \$0.15 per in.³, how much will it cost to rent a mailbox that is $4\frac{1}{2}$ in. by 12 in. by $5\frac{1}{2}$ in.?
- **25.** A box of staples has length $4\frac{1}{2}$ in., width $2\frac{1}{4}$ in. and height $\frac{3}{4}$ in. What is the greatest number of boxes of staples that can be shipped in a box measuring 9 in. by 18 in. with a height of 12 in.?



CACC Content Standards 6.G.1, 6.EE.2, 6.EE.2c Mathematical Practices MP.1, MP.5, MP.6

► Math and Construction



The Best Pool Construction Company is building a community swimming pool. The company has hired you and your associate to find how much tile and fencing needs to be ordered to finish the pool.

The pool is a rectangle 60 ft long and 20 ft wide. One third of the pool is 4 ft deep and the remaining part has a depth of 7 ft. There is to be a 3-ft wide tile deck around the entire pool and a safety fence around the entire area 11 ft from the edge of the tile deck.

1. What strategy will you use to find how much fence and tile is needed to finish the pool?



► Make a Drawing

Complete.

2. Use the information in the problem on Student Book page 277 to make a drawing at the right of a top view of the pool, tile, and fence. Label all the dimensions.

3. How many square feet of tile should be ordered for tile deck?

4. Safety fence is sold in 8-ft sections. How many sections should be ordered?

5. How many cubic feet of water will it take to fill the pool up to 6 in. below the top?



1. Select True or False for each statement.

1a.	Surface area and volume both measure the amount of space occupied by a solid figure.	○ True	○ False
1b.	Surface area and volume are measured using the same unit.	○ True	○ False
1c.	Surface area and volume are both attributes of solid figures.	○ True	○ False

2. Fill in the bubble next to the unit used to measure volume.

\circ square units \circ cubic units \circ linear units

Explain your answer choice in words or with a labeled sketch.

3. The volume of a rectangular pyramid can be found using the formula V = Bh.

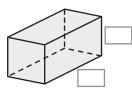
Part A: Use the tiles to show a different formula you can use to find the volume of a rectangular prism. You will not need to use every tile.





Part B: Explain how the two formulas are related, and why you can use either formula to find the volume of a rectangular prism.

4. The equation for the volume of the square prism is V = Mt. Label the prism.





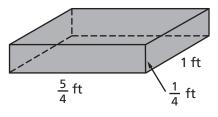
5. Choose one value from each column to make the volume of the rectangular prism true.

W	1
O 3	O 1
0 5	O 2
O 9	03
0 10	O 4

6. Use mental math to find the volume.



7. The volume of a prism can be found by packing it with unit cubes of the appropriate edge lengths.



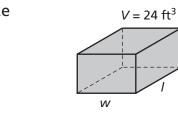
Part A

What is the longest edge length that would be appropriate for the unit cubes? Explain your answer.



Part B

If the longest dimension of the prism was $1\frac{1}{8}$ feet, would the length you chose in Part A be sensible? Explain.



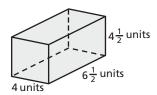
2 ft

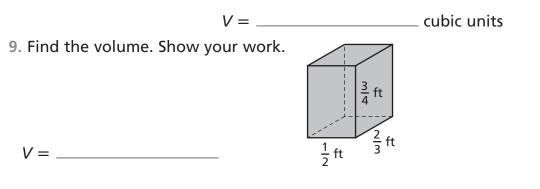


8. Cecilia used layers to find the volume of the prism below.

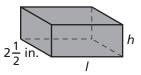
Part A Explain how to find the volume using layers.

Part B Use layers to find the volume of the prism.





10. The dimensions on the tiles below are values for *l* and *h*. For a prism with $w = 2\frac{1}{2}$ in., identify those expressions that will produce a volume of 270 in.³ and those that will produce a volume of 300 in.³



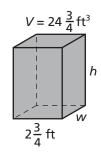
9 in. • 12 in.
$$2\frac{1}{2}$$
 in. • 48 in. 24 in. • $4\frac{1}{2}$ in.6 in. • 18 in.16 in. • $7\frac{1}{2}$ in.15 in. • 8 in. 20 in. • $5\frac{2}{5}$ in.

Volume: 270 in. ³	Volume: 300 in. ³



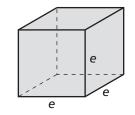
11. Choose one value from each column to make the volume of the rectangular prism true.

W	h
$^{-}$ 1 $\frac{1}{4}$	03
○ 1 <u>3</u>	O 4
O 2	○ 5
○ 2 <u>1</u>	0 6

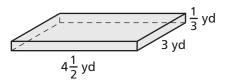


Select Yes or No to indicate if the equation represents the volume for the prism with sides *e*.

12a. $V = e \bullet e \bullet e$	\bigcirc Yes	\bigcirc No
12b. <i>V</i> = 3e	\bigcirc Yes	\bigcirc No
12c. $V = e^3$	○ Yes	○ No



13. Substitute the dimensions shown below into the volume formula to find the volume of the prism.Show your work.





14. Anthony labeled this rectangular prism.

Part A

Select the equations that represent the volume of the prism. Mark all that apply.

- $B \quad V = b \bullet b \bullet t$

Part B

Show your work. Find the volume of the prism if b = 3 cm and t = 7.5 cm.

15. Write an equation for the volume of the prism using the given variables.

V = _____

- 16. A gift box has a volume of 199 in.³ The area of the base of the box is $49\frac{3}{4}$ in.² What is the height?
 - h = _____

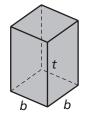
V =

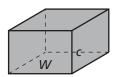
(**D**) $V = b^2 + t$

V =

17. A small pool in the shape of a rectangular prism has a length of $6\frac{1}{2}$ ft, a width of 5 ft and a height of 24 in. Jeb says the volume of the pool is 780 ft³.

Is Jeb correct? If he is, show how he may have found the volume. If not, explain what he did wrong and give the correct volume.







18. Choose Yes or No to indicate if the given dimensions represent a rectangular prism with a volume of 96 cubic inches.

18a. 2 in. • 6 in. • 8 in.	\bigcirc Yes	\bigcirc No
18b. 2 in. • 4 in. • 12 in.	○ Yes	\bigcirc No
18c. 4 in. • 12 in. • 4 in.	○ Yes	\bigcirc No
18d. 3 in. • 4 in. • 9 in.	○ Yes	\bigcirc No
18e. 4 in. ● 4 in. ● 6 in.	○ Yes	⊖ No

19. What is the volume of a rectangular prism with a base area of 52 square inches and a height of 14 inches? Show your work.

20. The volume of a rectangular prism is 6,037.5 cubic inches. The area of the base of the prism is 525 square inches. What is the height of the prism? Show your work.



21. John wants to place a layer of mulch on top of his 12 ft by 24 ft vegetable garden. If a 1.5 ft³ bag of mulch costs \$4, how much will it cost to place a 3-inch layer of mulch on the garden? Show your work.

V = -