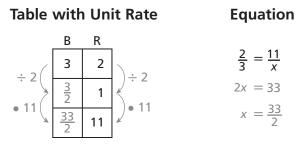


Dear Family,

In our math class we are studying ratios, rates, and percent. We will work with tables, diagrams and equations. These will help your child to develop her or his understanding of ratios, rates, and percent as well as to learn methods for solving problems. You can help your child by asking him or her to explain the tables, diagrams and equations.

Here are some examples of the kinds of problems we will solve and the kinds of tables, diagrams, and equations we will use.

• Purple Berry juice is made from 2 cups of raspberry juice for every 3 cups of blueberry juice. How many cups of blueberry juice are needed for 11 cups of raspberry juice?

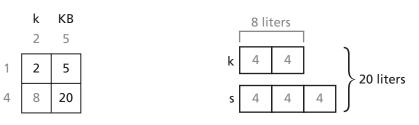


The answer is $\frac{33}{2}$ or $16\frac{1}{2}$ cups of blueberry juice.

• A juice company's KiwiBerry juice is made by mixing 2 parts kiwifruit juice with 3 parts strawberry juice. To make 20 liters of KiwiBerry juice, how much kiwifruit juice is needed?

Factor Puzzle

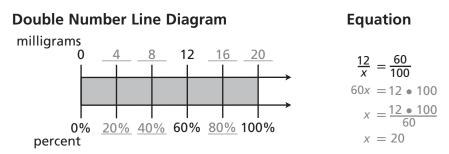
Tape Diagram



The answer is 8 liters of kiwifruit juice.



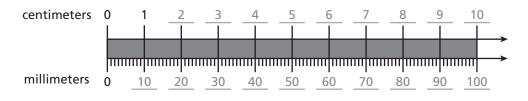
 If 12 milligrams of niacin is 60% of the recommended daily allowance for niacin, then what is the recommended daily allowance for niacin?



The answer is 20 milligrams.

• A double number line can be used to convert between centimeters and millimeters. Complete the double number line to show how centimeters and millimeters are related.

Double Number Line Diagram



If you have any questions or comments, please call or write to me.

Sincerely, Your child's teacher



CA CC

Unit 7 addresses the following standards from the *Common Core State Standards for Mathematics with California Additions*: 6.RP.1, 6.RP.2, 6.RP.3, 6.RP.3a, 6.RP.3b, 6.RP.3c, 6.RP.3d, 6.EE.6, 6.EE.7, 6.EE.9, 6.G.1, 6.G.4, and all Mathematical Practices.



Un vistazo general al contenido

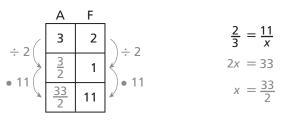
Estimada familia,

En la clase de matemáticas estamos estudiando razones, tasas y porcentajes. Para que su hijo logre una mejor comprensión de esos conceptos y aprenda métodos de resolución de problemas, trabajaremos con tablas, diagramas y ecuaciones. Usted puede ayudar, pidiéndole a su hijo o hija que le explique cómo usar las tablas, los diagramas y las ecuaciones.

Aquí tiene algunos ejemplos de los tipos de problemas que resolveremos y de los tipos de tablas, diagramas y ecuaciones que usaremos.

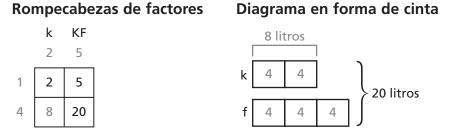
 Para hacer jugo azul se necesitan 2 tazas de jugo de frambuesa por cada 3 tazas de jugo de arándanos. ¿Cuántas tazas de jugo de arándanos se necesitan si se usan 11 tazas de jugo de frambuesa?

Tabla con tasa por unidad Ecuación



La respuesta es $\frac{33}{2}$ o $16\frac{1}{2}$ tazas de jugo de arándanos.

 Una compañía hace jugo de kiwi con fresa mezclando 2 partes de jugo de kiwi con 3 partes de jugo de fresa. Para hacer 20 litros, ¿cuánto jugo de kiwi se necesita?



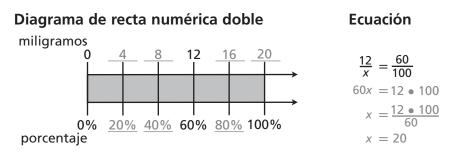


Un vistazo

general al

contenido

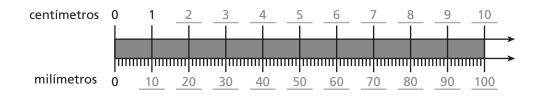
 Si 12 miligramos de niacina equivalen al 60% del consumo diario que se recomienda, entonces, ¿cuál es el consumo diario total de niacina que se recomienda?



La respuesta es 20 miligramos.

 Se puede usar una recta numérica doble para realizar conversiones entre centímetros y milímetros. Completen la recta numérica doble para mostrar cómo se relacionan los centímetros y los milímetros.

Diagrama de recta numérica doble



Si tiene comentarios o preguntas, por favor comuníquese conmigo.

Atentamente, El maestro de su hijo



En la Unidad 7 se aplican los siguientes estándares auxiliares, contenidos en los *Estándares estatales comunes de matemáticas con adiciones para California*: 6.RP.1, 6.RP.2, 6.RP.3, 6.RP.3a, 6.RP.3b, 6.RP.3c, 6.RP.3d, 6.EE.6, 6.EE.7, 6.EE.9, 6.G.1, 6.G.4, y todos los de prácticas matemáticas.



CACC Content Standards 6.RP.1, 6.RP.3, 6.RP.3a Mathematical Practices MP.4, MP.5, MP.6, MP.7, MP.8

Compare Paint Ratios

Grasshopper Green paint has a blue:yellow paint ratio of 2:7. Gorgeous Green paint has a blue:yellow ratio of 4:5.

You can **compare ratios**. You can find out which ratio makes paint that is more blue and which ratio makes paint that is more yellow.

To find out which paint is more blue, make the values for yellow the same. One way to do this is to make the value for yellow be the product of the yellow values in the basic ratios.

1. What is the product of the yellow values in the basic

ratios? _____

2. Complete these ratio tables.

| Grasshop | per Green |
|----------|-----------|
| Blue | Yellow |
| 2 | 7 |
| | 35 |

| Gorgeou | us Green |
|---------|----------|
| Blue | Yellow |
| 4 | 5 |
| | 35 |

3. Which paint is more blue? Why?

- 4. Which paint is less blue?
- 5. To find out which paint is more yellow, make the values for blue the same. Complete these ratio tables.

| Grasshop | per Green |
|----------|-----------|
| Blue | Yellow |
| 2 | 7 |
| | |

| Gorgeou | us Green |
|---------|----------|
| Blue | Yellow |
| 4 | 5 |
| | |

- 6. Which paint is more yellow?
- 7. Which paint is less yellow? ______

Vocabulary

compare ratios



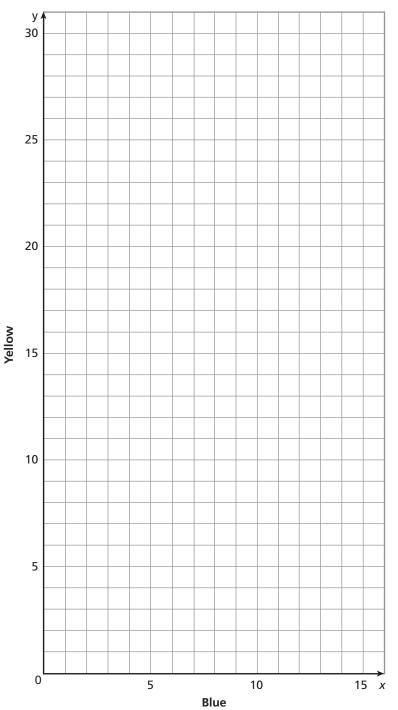
► Graph and Compare Paint Ratios

 Look back at the tables in Exercises 2 and 5 on page 271. Write the three ratios for each paint color in these tables.

| Grasshop | per Green |
|----------|-----------|
| Blue | Yellow |
| | |
| | |
| | |

| Gorgeou | us Green |
|---------|----------|
| Blue | Yellow |
| | |
| | |
| | |

9. Graph two points from each table. Draw and label a line for *Grasshopper Green* and a line for *Gorgeous Green*.



10. Discuss how the graphs can be used to decide which paint is more blue, less blue, more yellow, and less yellow.



CACC Content Standards 6.RP.1, 6.RP.2, 6.RP.3, 6.RP.3a, 6.RP.3b, 6.EE.6 Mathematical Practices MP.1, MP.2, MP.3, MP.7, MP.8

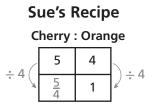
► Ratio as a Quotient

You can use a unit rate to describe *any* ratio. A unit rate for a ratio tells the amount of the first attribute for 1 unit of the second attribute.

Look again at Sue's and Ben's drink recipes.

Sue's recipe has 5 cups cherry juice and 4 cups orange juice. Ben's recipe has 6 cups cherry juice and 5 cups orange juice.

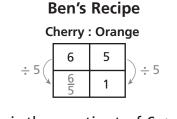
1. Find the amount of cherry juice in each drink for 1 cup of orange juice. Remember that when you divide both quantities in a ratio table by the same number, you get an equivalent ratio.



 $\frac{5}{4}$ is the quotient of $5 \div 4$.

Sue has $\frac{5}{4}$ cups of cherry juice for every cup of orange juice.

The unit rate for the ratio 5:4 is $\frac{5}{4}$.



 $_$ is the quotient of 6 \div 5.

Ben has _____ cups of cherry juice for every cup of orange juice.

The unit rate for the ratio ______ is

2. Find the amount of orange juice in each drink for 1 cup of cherry juice. This time use the orange:cherry ratio.

| S | ue's | Recip |)e |
|----|------|-------|----|
| Or | ange | Cherr | y |
| | 4 | 5 | |
| | | 1 | |

| Sue has | cup of orange juice for |
|-----------------|-------------------------|
| every cup of cl | herry juice. |

The unit rate for the ratio ______ is





Ben has _____ cup of orange juice for every cup of cherry juice.

The unit rate for the ratio ______ is



► Use Unit Rate Language to Describe Ratios

Complete each sentence using a fraction.

- **3.** Pedro uses a ratio of 7 quarts of blue paint to 4 quarts of white paint, a ratio of 7 to 4.
 - a. Pedro uses ______ quarts of blue paint for every quart of white paint.
 - **b.** The unit rate for the ratio 7:4 is ______.
- 4. Grandpa's soup uses 3 cups of tomatoes to 8 cups of broth, a ratio of 3 to 8.
 - a. Grandpa uses _____ cup of tomatoes for every cup of broth.
 - **b.** The unit rate for the ratio 3:8 is ______.
- 5. The unit rate for the ratio *a*:*b* (*b* not equal to 0) is ______.

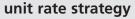
Compare Ratios Using Unit Rates

Look back at the unit rates you found on page 273 to answer these questions.

6. Whose drink is more cherry-flavored, Sue's or Ben's? How can you use unit rates to decide?

7. Whose drink is more orange-flavored, Sue's or Ben's? How can you use unit rates to decide?

Vocabulary



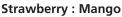


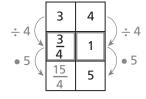
► The Unit Rate Strategy

You can use the **unit rate strategy** to find the unknown in a proportion problem.

 Maria's favorite juice recipe uses 4 cups of mango juice and 3 cups of strawberry juice. How many cups of strawberry juice should she mix with 5 cups of mango juice to make her favorite juice?

Since the unknown is the number of cups of *strawberry* juice, use the unit rate for the ratio *strawberry*:mango.





Answer: _____ cups

9. Adelina makes 2 drawings in her sketchbook while Jayden makes 5 drawings in his sketchbook. If both continue at their same constant rates, how many drawings will Adelina have made when Jayden has made 7 drawings?

Answer: _____ drawings

Solve. Use the unit rate strategy.

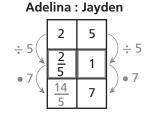
10. Diana can do 3 sit-ups in the time it takes Walter to do 2. How many sit-ups will Walter have done when Diana has done 12 sit-ups?

Answer: ______ sit-ups

11. Grandfather paid \$6 for 14 apples.If I buy the same kind of apples, how much will 35 apples cost?

Answer: _____

Since the unknown is the number of *Adelina's* drawings, use the unit rate for the ratio *Adelina*:Jayden.



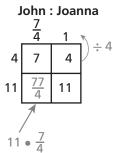


► Variations on the Unit Rate Strategy

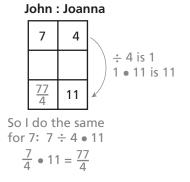
12. Gen, Claire, and Joey all use the unit rate strategy to solve this problem. But they record their thinking in different ways. Discuss how their methods are alike and how they are different.

> John can plant 7 tomato vines in the time it takes Joanna to plant 4 tomato vines. At that rate, when Joanna has planted 11 tomato vines, how many has John planted?

- a. *Gen*: I use a ratio table. First I divide and then I multiply.
 - John : Joanna $\div 4 \left(\begin{array}{c} 7 & 4 \\ \hline 7 & 4 \\ \hline 7 & 1 \\ \hline 7 & 1 \\ \hline 77 & 11 \\ \hline 77 & 11 \\ \hline \end{array} \right) \div 4$ • 11
- b. Claire: I make a Factor Puzzle and put the unit rate on top.



c. Joey: I "go through 1." I don't even write the unit rate.



Answer: $\frac{77}{4}$ tomato vines

Solve using any variation of the unit rate strategy.

13. Shawn plants 6 tulip bulbs in the time it takes Martin to plant 7 tulip bulbs. How many tulip bulbs will Shawn have planted when Martin has planted 21 bulbs?

Answer: _____

14. Amanda buys 3 pounds of blueberries for \$12. At the same price per pound, how much will 8 pounds of blueberries cost?

Answer: _____



CACC Content Standards 6.RP.1, 6.RP.2, 6.RP.3, 6.RP.3a, 6.RP.3b Mathematical Practices MP.1, MP.2, MP.4, MP.5, MP.7, MP.8

► Horizontal Ratio Tables

1. Complete the ratio table.

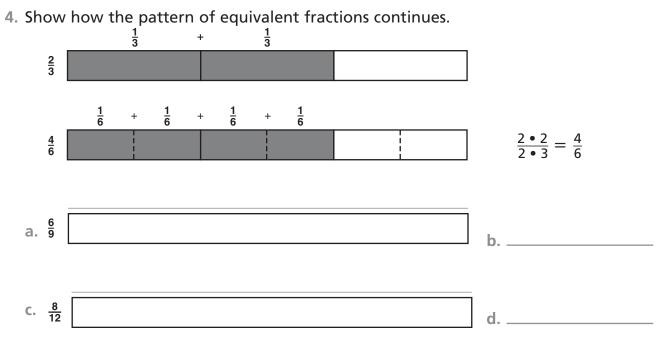
| | | | | Cups o | of Juice | | |
|------|---|----------------------|---|------------------|------------|-----------|--------|
| Tar | ngerine | | | 1 | 8 | | |
| | Cherry | \bigcirc | 1 | | 6 | 15 | 2 |
| | | asic ratio | | , | | | |
| b. | | are f cherry j | | ıps of taı | ngerine j | uice for | every |
| C. | The b | asic ratio | o of $\frac{che}{tange}$ | erry erine is | | | |
| d. | | is rine juice | | of cherr | y juice fo | or every | cup of |
| 2. A | 2. A flower mix has 21 tulips and 14 daffodils. | | | | | | |
| a. | The ba | asic ratio | o of $\frac{\text{tuli}}{\text{daffe}}$ | ps odils is | | | |
| b. | b. There are tulips for every daffodil. | | | | | | |
| C. | The ba | asic ratio | o for <u>daff</u> tul | odils is | | | |
| d. | There | is | daf | fodil for | each tul | ip. | |
| e. | | the basi d with 6 | | | y tulips | would b | e |
| f. | | the basi d with 6 | | now man | y daffoo | lils woul | d be |

Solve.

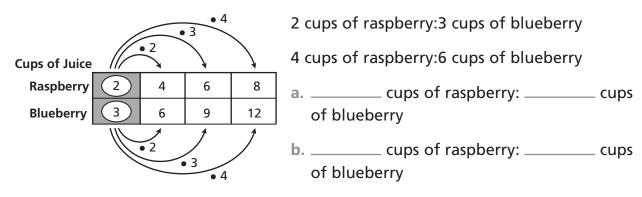
3. At the farm the ratios of mothers to baby sheep in each field are equivalent. If there are 20 mothers and 24 babies in the small field, how many babies are with the 45 mothers in the large field?



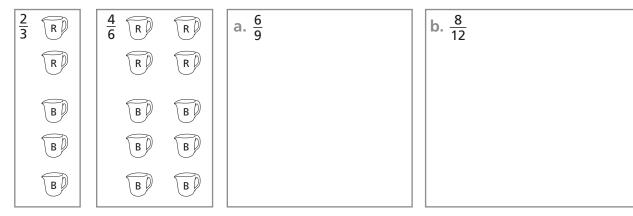
► Equivalent Fractions and Equivalent Ratios



5. Show how the pattern of equivalent ratios continues.



6. Draw to show the ratio pattern.



7. Discuss how equivalent fractions and equivalent ratios are alike and different.

296 UNIT 7 LESSON 3



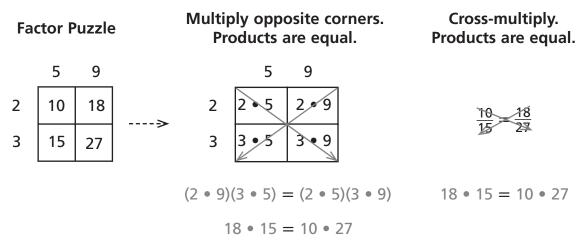
CACC Content Standards 6.RP.3, 6.RP.3b, 6.EE.6, 6.EE.7 Mathematical Practices MP.1, MP.3, MP.6, MP.7

Vocabulary cross-multiplication

Understanding Cross-Multiplication

When two equivalent ratios are written in a Factor Puzzle, the products of the numbers in opposite corners are equal. This results in a strategy for solving proportions called **cross-multiplication**.

 $\frac{10}{15} = \frac{18}{27}$



Cross-multiply to write an equation. Then, solve for the unknown.

1. $\frac{10}{15} = \frac{18}{9}$ 2. $\frac{8}{p} = \frac{14}{21}$ 3. $\frac{10}{25} = \frac{t}{15}$ 4. $\frac{s}{40} = \frac{10}{16}$ 18 • 15 = 10q

q = _____ p = _____ t = _____ s = _____

c = _____

Write the ratios in each proportion in fraction form. Then, solve by using cross-multiplication.

5. 16:20 = 12:*a* **6.** 18:*b* = 27:33 **7.** 6:15 = c:20 **8.** *d*:9 = 4:6

b = _____

a = _____

d = _____



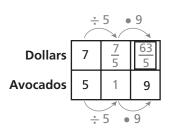
Cross-Multiplication and Unit Rates

 Zander paid \$7 for 5 avocados. How much would 9 avocados cost?

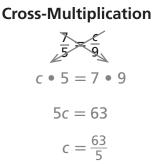
Discuss how these solution strategies relate to each other.

Rate Table



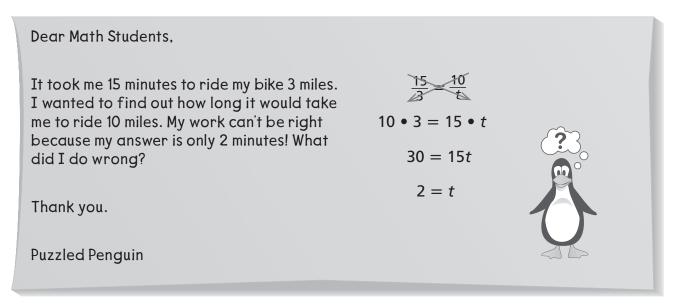






The price for 9 avocados is $\frac{63}{5}$ dollars, or \$12.60.

► What's the Error?



10. Write a response to the Puzzled Penguin.



CACC Content Standards 6.RP.1, 6.RP.3, 6.RP.3b, 6.EE.6, 6.EE.7 Mathematical Practices MP.1, MP.3, MP.4, MP.6

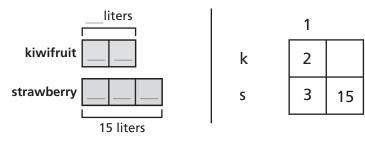
► Using Tape Diagrams to Model Ratios

A juice company's KiwiBerry juice is made by mixing 2 parts kiwifruit juice with 3 parts strawberry juice.

The ratio of parts of kiwifruit juice to parts of strawberry juice can be modeled by using a **tape diagram**.

Solve each problem three ways: using the tape diagram, using a Factor Puzzle, and using cross-multiplication.

 How many liters of kiwifruit juice should be mixed with 15 liters of strawberry juice to make KiwiBerry juice?





tape diagram

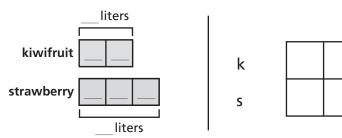




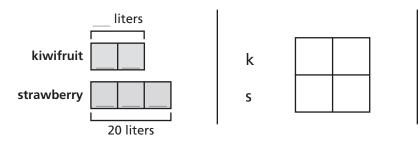
_____ liters



How many liters of strawberry juice should be mixed with
 50 liters of kiwifruit juice to make KiwiBerry juice?



3. How many liters of kiwifruit juice should be mixed with20 liters of strawberry juice to make KiwiBerry juice?_____ liters





► Using Tape Diagrams to Model Ratios (continued)

To make Perfect Purple paint, blue paint and red paint are mixed in a ratio of 3 to 5.

Solve each problem three ways: using a tape diagram, using a Factor Puzzle, and using cross-multiplication.

4. How many liters of red paint should be mixed with21 liters of blue paint to make Perfect Purple paint? ______ liters

5. How many liters of blue paint should be mixed with23 liters of red paint to make Perfect Purple paint?

Choose a method to solve.

6. To make bricks, you can mix clay and sand in a ratio of 2 to 3. How much clay do you need to mix with 10 cubic yards of sand?



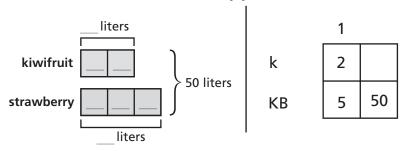
► Part-to-Whole Ratios

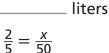
Remember that KiwiBerry juice is made by mixing 2 parts kiwifruit juice with 3 parts strawberry juice.

We can solve problems involving the total amount of juice or the total number of parts.

Solve each problem three ways: using the tape diagram, using a Factor Puzzle, and using cross-multiplication.

7. How many liters of kiwifruit juice should be used to make 50 liters of KiwiBerry juice?

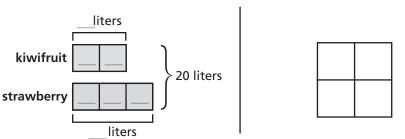




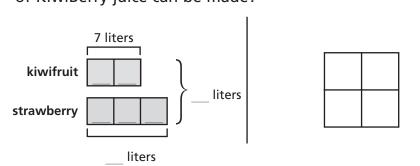
liters

liters

| 8. | How many liters of strawberry juice should be use | d |
|----|---|---|
| | to make 20 liters of KiwiBerry juice? | |



9. If 7 liters of kiwifruit juice are used, how many liters of KiwiBerry juice can be made?





► Part-to-Whole Ratios (continued)

To make Perfect Purple paint, blue paint and red paint are mixed in a ratio of 3 to 5.

Solve each problem three ways: using a tape diagram, using a Factor Puzzle, and using cross-multiplication.

10. How much red paint is needed to make 20 liters of Perfect Purple paint?

_____ liters

11. If 10 liters of blue paint are used, how many liters of Perfect Purple paint can be made?

_____ liters

Choose a method to solve.

12. To make bricks, you can mix clay and sand in a ratio of 2 to 3. To make 55 cubic feet of the mixture, how much sand do you need to use? How much clay do you need to use?



CACC Content Standards 6.RP.1, 6.RP.2, 6.RP.3, 6.RP.3b, 6.EE.6, 6.EE.7 Mathematical Practices MP.1, MP.2, MP.3, MP.6, MP.7

- ► Different Ways to Describe Ratios
- Seth made a sand mixture by mixing 4 parts green sand with 3 parts yellow sand.

| green | | |
|--------|--|--|
| yellow | | |

Complete each sentence to describe the green sand to yellow sand ratio.

1. The mixture is _____ parts green sand and

_____ parts yellow sand.

2. Green sand and yellow sand are mixed in a ratio of

_____ to _____ or _____: _____.

3. For every _____ cups of green sand, there are

_____ cups of yellow sand in the mixture.

Complete each sentence to describe the green sand to total ratio.

- 4. There are _____ parts green sand in _____ parts total mixture.
- 5. Green sand and total mixture are in a ratio of _____

to _____ or _____ : _____.

6. For every _____ cups of green sand, there are

_____ cups of mixture.

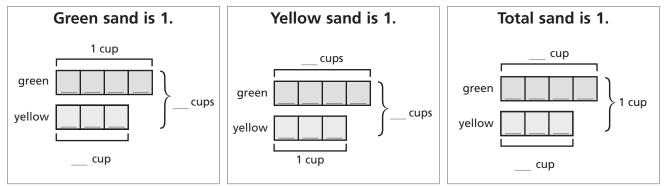
Describe the yellow sand to total ratio in three ways.

| 7. | |
|----|--|
| | |
| 8. | |
| 9. | |
| | |



Different Portions Can Be One Whole

10. Complete each tape diagram.



Unit Rates

Write a fraction to complete each unit rate.

- 11. _____ cup of yellow sand for every 1 cup of green sand in the mixture
- 12. _____ cups of green sand for every 1 cup of yellow sand in the mixture
- 13. _____ cup of green sand and _____ cup of yellow sand for every 1 cup of mixture
- 14. _____ cups of mixture for every 1 cup of green sand
- 15. _____ cups of mixture for every 1 cup of yellow sand

Multiplicative Comparisons

Write a fraction to complete each multiplicative comparison.

- **16.** The amount of yellow sand is ______ times the amount of green sand.
- 17. The amount of green sand is ______ times the amount of yellow sand.
- **18.** The total amount of mixture is ______ times the amount of green sand.
- **19.** The total amount of mixture is ______ times the amount of yellow sand.

Vocabulary

multiplicative comparison



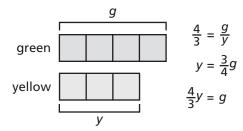
► What's the Error?

| Dear Math Students. I made my own sand mixture. I mixed 2 parts purple and 5 parts orange. |
|--|
| purple |
| orange |
| Then I wrote this multiplicative comparison. |
| • The amount of purple sand is $\frac{2}{5}$ times the amount of the total mixture. |
| My friend says that I made a mistake. Did I? If I did, can you tell me what mistake I made and help me correct it? |
| Your friend, |
| Puzzled Penguin |
| |

20. Write a response to Puzzled Penguin.



21. Let g be the number of cups of green sand in Seth's ratio. Let y be the number of cups of yellow sand in Seth's ratio.



Discuss why these three equations can all be used to relate g and y.



► Blue-and-Red Mixtures

22. Make up your own blue-and-red sand mixture.Your mixture should have a total of 5 parts. Draw a tape diagram to show the ratio of blue to red.

23. Describe the ratio of blue sand to red sand in three ways.

24. Describe the ratio of blue sand to the total mixture in three ways.

- **25.** Write two sentences that use a fraction to compare the amounts of the two colors. Use the words *times as much*.
- 26. Suppose you make a large batch of your blue-and-red sand mixture. Let b be the number of cups of blue sand that you use, and let r be the number of cups of red sand that you use. Write three equations relating b and r.
- **27.** How is your mixture different from a mixture with the same colors mixed in a different ratio?



CACC Content Standards 6.RP.1, 6.RP.3, 6.RP.3a, 6.RP.3b Mathematical Practices MP.1, MP.3, MP.6

► Practice Solving Rate and Ratio Problems

Solve. Use different methods including tables, Factor Puzzles, cross-multiplication, and tape diagrams. Look for the problems that cannot be solved with any of these!

- In a lab, Chemical 1 and Chemical 2 are mixed in a ratio of 4 to 5. How much of Chemical 1 is needed to mix with 35 liters of Chemical 2?
- 2. In a lab, Chemical 1 and Chemical 2 are mixed in a ratio of 4 to 5. How much of each chemical is needed to make 35 liters of the mixture?

Chemical 1: _____ Chemical 2: _____

- Pokey the snail travels 25 centimeters every
 2 minutes. How far will Pokey go in 15 minutes?
- 4. When Gary the snail travels at a steady rate of 15 centimeters per minute, it takes him 6 minutes to get from the pineapple to the rock. How long will it take Gary to get from the pineapple to the rock if he travels at a steady rate of 30 centimeters per minute?
- 5. At a factory, an assembly line produces 100 cans every 3 minutes. How long will it take the assembly line to produce 250 cans?
- 6. At a factory, an assembly line produces 100 cans every 3 minutes. How many cans will the factory produce in 8 hours?

Show your work.



► Practice Solving Rate and Ratio Problems (continued)

7. At a factory, each assembly line produces 100 cans every 3 minutes. If two assembly lines are working, how many cans will they produce in 15 minutes? Show your work.

- 8. It takes Brittany 2 hours to mow 5 acres of grass. At that rate, how long would it take Brittany to mow 8 acres?
- 9. It takes Brittany 2 hours to mow 5 acres of grass. If Austin mows grass at the same rate as Brittany, how long will it take the two of them working together to mow 15 acres of grass?
- 10. Jorge and Ryan are running laps around the track. Jorge runs 5 laps for every 4 laps that Ryan runs. When Ryan has run 15 laps, how many laps will Jorge have run?
- 11. At a perfume factory, fragrance designers are mixing musk oil and spice cologne in different ratios.Mixture 1 is 2 parts musk oil to 5 parts spice cologne.Mixture 2 is 3 parts musk oil to 7 parts spice cologne.Which will have more of a spice fragrance? Explain.
- 12. Fragrance designers make Roselily perfume by mixing rose and lily perfumes. In Roselily perfume, the amount of rose is $\frac{2}{5}$ times as much as the amount of lily. What is the ratio of rose to lily in Roselily? Draw a tape diagram to show the ratio.



CACC Content Standards 6.RP.3, 6.RP.3c Mathematical Practices MP.1, MP.2, MP.3, MP.4, MP.6, MP.8

Vocabulary

percent

Define Percent

Percent means "out of 100" or "for each 100." The symbol for percent is %.

37% is read "37 percent." It can mean the fraction $\frac{37}{100}$, the ratio 37:100, or the rate 37 *per* 100.

The fans at a sold-out concert are in 100 equal sections of seats. Each small rectangle in the diagram represents one section of fans.

1. Color one section blue.

What fraction of the fans is this?

What percent of the fans is this?

3. Color 23% of the sections green.

What fraction of the fans is this?

2. Color three sections red.

What fraction of the fans is this?

What percent of the fans is this?

4. Color 37% of the sections yellow.

What fraction of the fans is that?

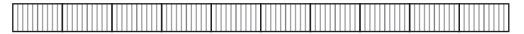
5. Shade some sections in purple. What percent did you shade?



► Percents of Bar Diagrams

The bars in Exercises 6–9 are divided into 100 equal parts.

6. Shade 5% of the bar.



7. Shade 15% of the bar.



8. Shade 45% of the bar.

9. Shade 85% of the bar.



10. Label each section with the percent of the whole bar it represents. Under the section, write the fraction it represents.

Bar A

| % | % |
|---|---|
| | 1 |

Bar B

| % | % | % | % | % | % | % | % | % | % |
|-------|---|---|---|---|---|---|---|----|---|
| | | | • | | | | - | •; | |
| | | | | | | | | | |
| Bar C | | | | | | | | | |
| | % | | % | | % | | % | | % |
| | | 1 | | 1 | | 1 | | | |
| | | | | | | | | | |
| Bar D | | | | | | | | | |
| | % | | % |) | | % | | % |) |

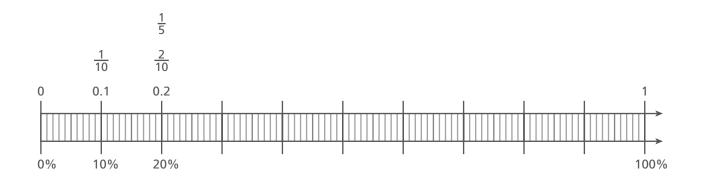
11. Shade 70% of Bar B. **12.** Shade 60% of Bar C.

13. Shade 75% of Bar D.



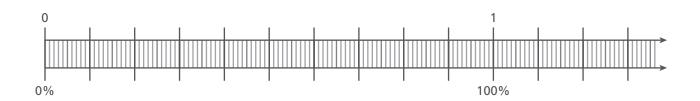
► Relating Percents, Decimals, and Fractions

14. Label each long tick mark with a decimal, a percent, and a fraction with a denominator of 10. If the fraction can be simplified, write the simplified form as well.



15. Write each percent as a fraction with denominator 100 and as a decimal. Then place the percents and decimals on the number lines.

| Percent | 83% | 51% | 46% | 6% | 60% | 27% | 127% | 3% | 30% | 130% |
|----------|------------------|-----|-----|----|-----|-----|-------------------|----|-----|------|
| Fraction | <u>83</u> 100 | | | | | | <u>127</u> 100 | | | |
| Decimal | 0.83 | | | | | | 1.27 | | | |





► What's the Error?

Dear Math Students,

I said that 7% is 0.7, but my friend said that I am not right. Why not? Please help me understand how percents and decimals are related.

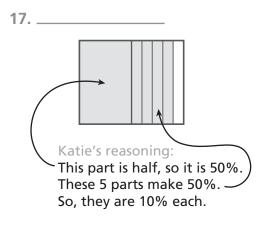
Thank you.

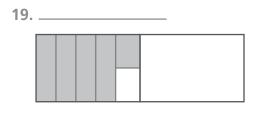
Puzzled Penguin

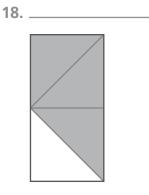


Percents and Area

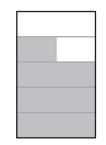
What percent of the figure is shaded?







20. _____





CACC Content Standards 6.RP.3, 6.RP.3c, 6.EE.6, 6.EE.7 Mathematical Practices MP.1, MP.3, MP.4, MP.6

► Model Finding a Percent of a Number

The 300 students at a school are in 100 groups of 3.

| * ** | ? ?? ? ?? | *** | *** | ? ? ? ? | ** * | * ** | * ** |
|----------------------|-------------------------|-----|--------------|----------------|-------------|--------------|-------------|
| *** *** | *** | *** | *** | * ** | *** | *** | *** |
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| *** | ????????????? | *** | *** | ? ?? | *** | ? ?? | ** * |
| * ** * | *** | *** | % % % | ? ?? | *** | ** * | ** * |
| *** | ? ?? ? ?? | *** | *** | ? ?? | *** | X X X | * ** |
| * ** | ????????????? | *** | *** | ? ?? | *** | ** * | ? ?? |
| *** | *** | *** | *** | * ** | * ** | ** * | * ** |

1. Color one group blue.

What percent of the students is this?

2. Color four groups red.

What percent of the students is this?

What number of students is this?

3. Color 17 groups green.

What percent of the students is this?

What number of students is this?

5. Color 24% of students orange.

What number of students is this?

What number of students is this?

4. Color 9% of the students yellow.

What number of students is this?

Color 35% of the students purple.
 What number of students is this?



► Find a Percent of a Number

Three students had different ideas about how to solve the following problem.

Of the 300 students at a school, 35% say they are going on a field trip. How many students are going on the field trip?

Use each idea to solve the problem.

- 7. Anna's idea: I will divide 300 by 100 to find 1% of 300. Then, I will multiply that answer by 35 to find 35% of 300.
- 8. Rantavious's idea: I will use the fact that 35% of 300 means $\frac{35}{100}$ times 300.
- 9. Jon's idea: If f is the number of students going on the trip, then the fraction of students going is $\frac{f}{300}$, and it is also $\frac{35}{100}$. I can write and solve a proportion.
- 10. What is 80% of 300 students? Solve in two ways.
- 11. What is 26% of 1,200 students? Solve in two ways.

Show your work.



► Percent as a Ratio

Now the students at the school are in 3 groups of 100.

| \$\$\$\$\$ \$\$\$\$ | \$\$\$\$\$ \$\$\$\$\$ | \$\$\$\$\$ \$\$\$\$\$ |
|----------------------------|------------------------------|------------------------------|
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12. Circle one student from each group in blue.

What percent of the students is this?

What number of students is this?

14. Circle 45% of the students in green.

How many students is this? Why?

13. Circle four students from each group in red.

What percent of the students is this?

What number of students is this?

15. Circle 82% of the students in yellow.

How many students is that? Why?



► Methods for Finding a Percent of a Number

Five students had different ideas about how to solve the problem below.

Of the 300 students at a school, 99% say they are going to the school party. How many students is this?

Use each idea to solve the problem.

16. Hilda's idea: 99% means 99 for each 100. So, I will use a 99% ratio table.

Show your work.

99% ratio table portion 99 whole 100 200 300

- 17. Anna's idea: I will divide 300 by 100 to find 1% of 300.Then, I will multiply that answer by 99 to find 99% of 300.
- **18. Rantavious's idea:** I will use the fact that 99% of 300 means $\frac{99}{100}$ times 300.
- **19.** Jon's idea: If *p* is the number of students going to the party, then the fraction of students going is $\frac{p}{300}$, and it is also $\frac{99}{100}$. I can write and solve a proportion.
- 20. Gregory's idea: 99% is 100% minus 1%, so I will take 1% of the 300 students away from 100% of 300.

Solve.

21. What is 51% of 600 students?

22. What is 49% of 500 students?



CACC Content Standards 6.RP.3, 6.RP.3c, 6.EE.6, 6.EE.7 Mathematical Practices MP.1, MP.2, MP.3, MP.4, MP.8

Percents of Numbers

The adult dose of a medicine is 8 milliliters. The child dose is 75% of the adult dose. How many milliliters is the child dose?

- Complete the double number milliliters 0 _____ 8 line to help you solve this problem.
 Discuss and complete these percent 0% _____ 100%
- solutions.



Trey's Reasoning About Parts

100% is 4 parts, which is 8 mL.

25% is 1 part, which is 8 mL \div 4 = 2 mL.

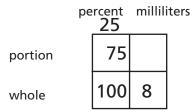
75% is 3 parts and is _____

Tomaslav's Equation

m is 75% of 8.

$$m = \frac{75}{100} \bullet 8 =$$

Quowanna's Factor Puzzle



Jessica's Proportion

| | percent | | milliliters |
|------------------|------------------|---|---------------|
| portion whole | <u>75</u> 100 | = | <u>m</u> 8 |
| | <u>3</u> 4 | = | <u>m</u> 8 |
| | т | = | |

Solve in two ways.

- 3. The adult dose of a medicine is 6 milliliters. The child dose is 75% of the adult dose. How many milliliters is the child dose?
- 4. A chemist needs 20% of the 120 milliliters of solution in a beaker. How many milliliters of solution does the chemist need?



Find the Whole from the Percent and the Part

If 12 milligrams is 60% of the recommended daily allowance for niacin, then what is the recommended daily allowance for niacin?

| Complete the double number milligran line to help you solve this problem. | ns 0 12 |
|---|---|
| 6. Discuss and complete these perce solutions. | nt 0% 60% 100% |
| Trey's Reasoning about Parts | Quowanna's Factor Puzzle |
| 60% is 3 parts and is 12 mg. | percent milliliters |
| 20% is 1 part, which is 12 mg \div 3 = 4 mg. | portion 60 12 |
| 100% is 5 parts, which is | whole 100 |
| Tomaslav's Equation | Jessica's Proportion |
| 60% of g is 12. | percent milliliters |
| $\frac{60}{100} \bullet g = 12$ | portion $\frac{60}{100} = \frac{12}{g}$ |
| | I |

Solve.

- 7. A chemist poured 12 mL of chemicals into water to make a solution. The chemicals make up 80% of the solution. How many milliliters is the full solution?
- 8. What is 40% of 70? _____ 9. 40% of what number is 70? _____

10. 30% of what number is 120? _____ 11. What is 30% of 120? _____

12. If 75% of the recommended daily allowance of vitamin C is 45 mg, what is the recommended daily allowance of vitamin C?



CACC Content Standards 6.RP.3, 6.RP.3c, 6.EE.6, 6.EE.7 Mathematical Practices MP.1, MP.6, MP.8

► Use Percents to Compare

Using percents can help you compare two groups when the sizes of the groups are different.

Appling School has 300 students and 45 students ride a bus to and from school each day. Baldwin School has 500 students and 55 students ride a bus.

1. Discuss and complete these methods for calculating the percent of students at Appling School who ride a bus.

| Alex's Equation | Jordan's Equation |
|----------------------------------|----------------------------------|
| <i>f</i> % is $\frac{45}{300}$. | <i>f</i> % of 300 is 45. |
| $\frac{f}{100} = \frac{45}{300}$ | $\frac{f}{100} \bullet 300 = 45$ |
| | |

Aliya's Factor Puzzle

percent students

portion

whole

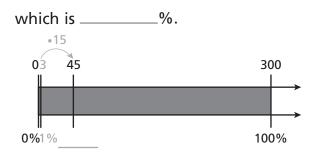


Rachel's Idea of Going through 1%

300 students is 100%.

 $300 \div 100 = 3$; 3 students is 1%.

 $45 \div 3 = 15$; 45 students is 15 groups of 3 students,



2. Use two methods to calculate the percent of students at Baldwin School who ride a bus.



Solve.

► Mixed Percent Problems

- **3.** 26 is what percent of 130?
 4. 25% of what number is 225?
- 5. What is 75% of 280? _____ 6. 70% of what number is 595? _____

Show your work.

7. A company spent \$4,500 of its \$18,000 advertising budget on Internet ads. What percent of its advertising

budget did the company spend on Internet ads?

- 8. If 30% of a company's advertising budget is \$7,200, then what is the full advertising budget?
- Another company's advertising budget is \$7,200. The company spent 30% of their budget on newspaper ads. How much did the company spend on newspaper ads?
- **10.** If a gasoline-ethanol mixture made with 24 liters of ethanol is 15% ethanol, then how many liters is the whole mixture?
- 11. If 3 gallons of antifreeze is mixed with 2 gallons of water, what percent of the mixture is antifreeze?

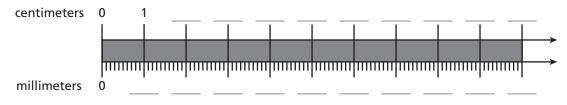
What percent of the mixture is water?

12. If a pharmacist needs to mix 800 mL of antibiotic with water so that the mixture is 40% antibiotic, then how much water does the pharmacist need to add?



CACC Content Standards 6.RP.3, 6.RP.3d, 6.EE.6, 6.EE.7, 6.G.1, 6.G.4 Mathematical Practices MP.1, MP.3, MP.4, MP.6, MP.8

- Convert Between Centimeters and Millimeters
- 1. Label the double number line to show how centimeters (cm) and millimeters (mm) are related.



We can write two unit rates comparing centimeters to millimeters.

There are 10 millimeters per centimeter.

We can write this unit rate as $10 \frac{\text{mm}}{\text{cm}}$.

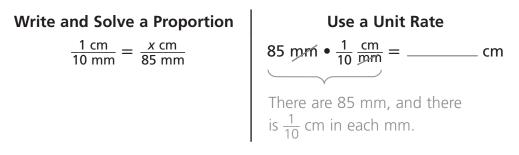
```
There is \frac{1}{10} centimeter per millimeter.
We can write this unit rate as \frac{1}{10} \frac{\text{cm}}{\text{mm}}.
```

Unit rates are helpful for converting measurements from one unit to another.

2. Compare these methods of converting 52 centimeters to millimeters.

Write and Solve a ProportionUse a Unit Rate $\frac{1}{10} \text{ mm} = \frac{52}{x} \text{ cm}$ $52 \text{ cm} \cdot 10 \frac{\text{mm}}{\text{cm}} = 520 \text{ mm}$ The unit cm
cancels, leaving
the unit mm. $52 \cdot 10 = 1 \cdot x$ There are 52 cm, and there are
10 mm in each cm.The unit mm.

3. Complete these methods for converting 85 millimeters to centimeters.



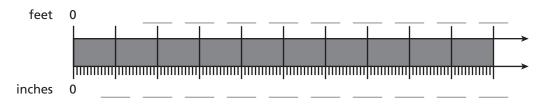
So, 85 mm = _____ cm. UNIT 7 LESSON 12

So, 52 cm = 520 mm.



Convert Between Feet and Inches

4. Label the double number line to show how feet and inches are related.



5. What are the two unit rates in this situation?



- Convert 132 inches to feet by multiplying by a unit rate.
 Show your work.
- 7. Convert $6\frac{1}{2}$ feet to inches by multiplying by a unit rate. Show your work.

132 in. = _____ ft

 $6\frac{1}{2}$ ft = _____ in.

Practice Converting Units of Length

- 8. What two unit rates relate centimeters (cm) and meters (m)?
- 9. Convert 7.9 meters to centimeters using any method.10. Convert 42 centimeters to meters using any method.

```
7.9 m = _____ cm
```

| using any method. | | |
|-------------------|---|---|
| 42 cm = _ | r | n |

- 11. What two unit rates relate feet (ft) and yards (yd)?
- Convert 16 feet to yards using any method.
- **13.** Convert 24 yards to feet using any method.

16 ft = _____ yd

24 yd = _____ ft



► Find Area When Units Are Different

Riley and Kelsey wanted to find the area of their rectangular bedroom. Riley measured the length and Kelsey measured the width. They made the sketch at the right to show their measurements.

Below are the girls' area calculations.

Riley's Calculation

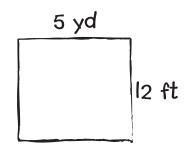
I want to find the area in square yards, so I have to change 12 feet to yards.

12 ft •
$$\frac{1}{3} \frac{\text{yd}}{\text{ft}} = 4 \text{ yd}$$

Now, I can use the area formula.

$$A = Iw = 4 \text{ yd} \bullet 5 \text{ yd} = 20 \text{ yd}^2$$

- 14. Discuss Riley and Kelsey's calculations.
- **15.** Explain how the diagram at the right shows that $1 \text{ yd}^2 = 9 \text{ ft}^2$.



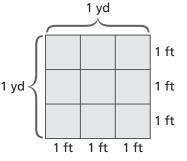
Kelsey's Calculation

I want to find the area in square feet, so I have to change 5 yards to feet.

5 yd • 3
$$\frac{ft}{yd} = 15$$
 ft

Now, I can use the area formula.

$$A = Iw = 15 \text{ ft} \cdot 12 \text{ ft} = 180 \text{ ft}^2$$



16. Write two unit rates relating square yards and square feet.

 $\underline{\qquad} \frac{ft^2}{yd^2} \text{ and } \underline{\qquad} \frac{yd^2}{ft^2}$

17. Use one of the unit rates from Exercise 16 to convert Riley's area of 20 yd² to square feet. Does the answer agree with the area Kelsey got?

20 yd² = _____

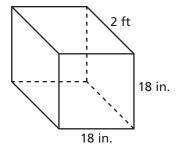


► Practice Solving Area Problems

Solve.

Show your work.

- 18. A rectangle has a base length of 3 meters and a height of 15 decimeters. Find the area of the rectangle. Be sure to specify the unit in your answer.
- **19.** Find the surface area of the rectangular prism at the right. Be sure to specify the unit in your answer.



► What's the Error?

Dear Math Students,

The school nurse said that I am 42 inches tall. I wanted to figure out how many feet this is. Here's what I did:

42 in. • $12 \frac{\text{in.}}{\text{ft}} = 504 \text{ ft}$

I know I am not 504 feet tall! Please help me figure out what I did wrong and help me find my real height in feet.

Thank you.

Puzzled Penguin

20. Write a response to Puzzled Penguin.





CACC Content Standards 6.RP.3, 6.RP.3d, 6.EE.6, 6.EE.7 Mathematical Practices MP.3, MP.6

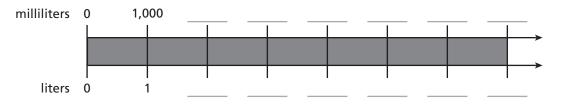
Vocabulary

liquid volume

Converting Metric Units of Liquid Volume

The most common metric units of **liquid volume**, or capacity, are milliliters and liters.

1. Label the double number line to show how liters (L) and milliliters (mL) are related.



- 2. What two unit rates relate liters and milliliters?
- **3.** A can holds 344 mL of seltzer. How many liters is this? Find your answer in two ways: by writing and solving a proportion and by using a unit rate.

Write and Solve a Proportion

Use a Unit Rate

344 mL = _____ L

Solve using any method.

- **4.** A bottle contains 1.89 liters of water. How many milliliters is this?
- **5.** A soap dispenser holds 220 mL of soap. A refill bottle of soap contains 1.76 L. How many times can the dispenser be refilled from the bottle?



Converting Customary Units of Liquid Volume

Units of liquid volume, or capacity, in the customary system include cups, pints, quarts, and gallons.

- 6. Write two unit rates relating quarts (qt) and gallons (gal).
- 7. How many quarts would it take to fill a $2\frac{3}{4}$ -gallon punch bowl?
- 8. One of the cows on Tessa's farm produces an average of 22 quarts of milk each day. How many gallons is this?
- 9. How many pints are in 1 gallon?
- **10.** Use your answer to Question 9 to help you write two unit rates relating pints (pt) and gallons (gal).
- 11. The school cafeteria sells 300 half-pint cartons of milk every day. How many gallons of milk is this?
- **12.** Which is more, 72 cups or 20 quarts? Explain how you found your answer.

Customary Units of Liquid Volume

2 cups = 1 pint2 pints = 1 quart4 quarts = 1 gallon



Converting Units of Mass

The most common units of mass are grams (g) and kilograms (kg).

13. Complete.

1 kg = _____ g 1 g = ____ kg

14. Write two unit rates relating grams and kilograms.

15. Convert 3,575 grams to kg.

16. Convert 3,575 kg to grams.

3,575 g = _____ kg

3,575 kg = _____ g

17. A nickel has a mass of 5 g. A bag contains 2 kg of nickels. How many nickels are in the bag? Explain.

Converting Units of Weight

The most common units of weight are ounces (oz) and pounds (lb).

- **18.** There are 16 ounces in 1 pound. Write two unit rates relating ounces and pounds.
- 19. Convert 420 pounds to ounces. 20. Convert 420 ounces to pounds.

21. Donelle adopted two puppies. Daisy weighs $7\frac{1}{2}$ pounds. Bandit weighs 108 ounces. Which puppy weighs more? Explain.



► Conversion Word Problems

Solve.

Show your work.

- 22. A box of FruitBlaster cereal contains 450 g of cereal.
 - a. How many kilograms of cereal will the company need to fill 15,000 boxes?
 - **b.** How many boxes of FruitBlaster cereal can the company fill with 15,000 kg of cereal?
- 23. A perfume bottle holds 5 mL. The perfume company wants to fill 25,000 bottles. How many liters of perfume will the company need?
- 24. A restaurant has a viewing aquarium that holds70 gallons of water. How many cups is that amount of water equivalent to?
- 25. There are 75 sixth grade students at Wilson Middle School. Each student has a science book that is 5 cm thick. If all the sixth graders stacked their science books on top of each other, would the stack be as tall as the 4-meter-tall school building? Explain.



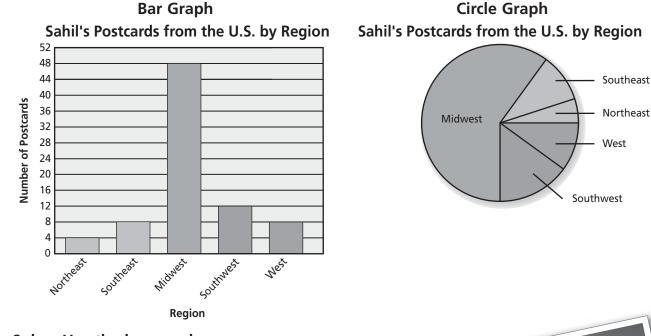
CACC Content Standards 6.RP.1, 6.RP.3c Mathematical Practices MP.1, MP.2, MP.3, MP.6

Vocabulary

bar graph circle graph

Math and Collections

The **bar graph** and the **circle graph** show data about Sahil's postcard collection.



Solve. Use the bar graph.

1. What is the ratio of cards from the Northeast to cards

from the West? _____

2. What is the ratio of cards from the West to cards from the Northeast?

Solve. Use the circle graph.

3. Are more or fewer than 50% of Sahil's cards from

the Midwest? _____

4. Are more or fewer than 25% of Sahil's cards from

the Southwest? _____

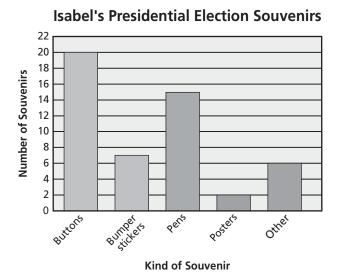
5. How could you check your answers to Problems 3 and 4 by using the bar graph?

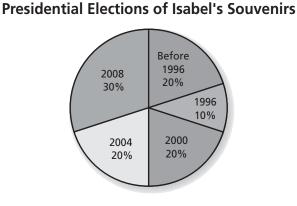




► Choose Graphs to Solve

Isabel has a collection of souvenirs from U.S. presidential elections. The graphs below show the kinds of souvenirs she has collected and the dates of the presidential elections for her souvenirs.





Solve. For Problems 6–8, write whether you used the bar graph, the circle graph, or both.

- 6. What percent of Isabel's souvenirs are buttons?
- 7. What percent of Isabel's souvenirs are from elections in 2000 or later?
- 8. How many of her souvenirs are from the 2008 election?
- 9. Hector says that the graphs make it clear that 6 of the buttons must be from the 2008 election. Do you agree? Explain.





1. Dotti's potato salad uses 5 large potatoes and 2 eggs. Choose True or False for each statement.

| 1a. The salad uses potatoes and eggs in a ratio of 5:2. | | 5:2. |
|---|-------------------------|---------------------------|
| | \odot True | \bigcirc False |
| 1b. The salad uses 2 potatoes for | every 5 eggs. O True | ○ False |
| 1c. The salad uses $\frac{5}{2}$ potatoes for | 0 | False |

2. How are comparing two fractions and comparing two ratios alike? How are they different?

| Alike: | | |
|------------|--|--|
| | | |
| Different: | | |
| | | |
| | | |

3. The double line graph shows that 100% of a quantity has a mass of 24 grams.

| Part A | grams | 0 | | | 24 |
|--|---------|----|---|---|--------|
| Complete the double number line and explain your method. | | | | | |
| | percent | 0% | I | • | 100% |

Part B

Explain how you can use the double number line to find 75% of 24 grams.



4. Fill in the bubble next to the measure that makes the sentence true.

There are 4 quarts in 1 gallon, so there are ______ gallons in 1 quart.

 $\bigcirc \frac{4}{1}$

| $\bigcirc \frac{1}{4}$ | - | \bigcirc | 0.4 |
|------------------------|---|------------|-----|
| 4 | | | |

5. Select Yes or No to indicate if the expression is equivalent to the ratio 3:2.

| 5a. $\frac{3}{2}$ | \circ Yes | \odot No |
|-------------------|-------------|---------------|
| 5b. 6:3 | \circ Yes | \circ No |
| 5c. <u>9</u> | \circ Yes | \odot No |
| 5d. 12:8 | \odot Yes | \bigcirc No |
| 5e. <u>2</u> | ○ Yes | \circ No |

- 6. There are 420 pumpkins in Jennifer's pumpkin patch. She picked 15% of them. How many pumpkins did Jennifer pick?
 - A 15 pumpkins
 - **B** 28 pumpkins
 - C 42 pumpkins
 - **D** 63 pumpkins
- 7. Carly buys 4 pounds of strawberries for \$9.00. What is the unit cost of the strawberries?



Choose numbers from the number tiles to write two fractions that will make the statement true. You may write a number more than once.

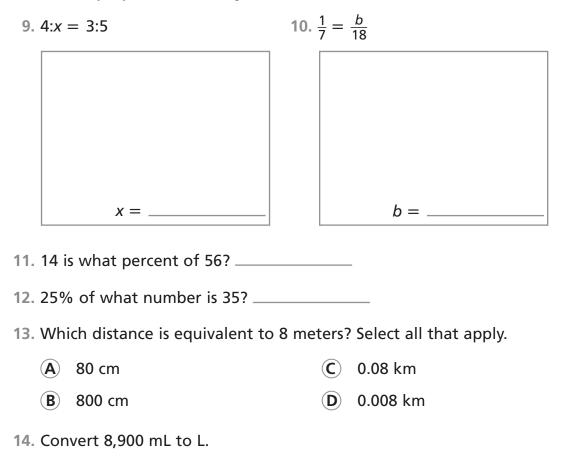


8. A paint mixture is 4 parts red and 5 parts white. For every 1 gallon of

paint, ______ gallon is red and ______ gallon is white.



Solve each proportion. Show your work.



15. Orange and pineapple juice are mixed in a ratio of 4 to 5. Choose one number from each column to show the amount of each juice that is needed to make 36 gallons of orange-pineapple juice.

| orange | pineapple |
|----------|-----------|
| O 12 gal | ○ 16 gal |
| O 16 gal | O 18 gal |
| O 18 gal | O 20 gal |
| ○ 20 gal | ○ 24 gal |

16. Savitri buys 3 pounds of sliced turkey for \$12. At that rate, how much sliced turkey can she buy for \$25? Show your work.

_____ pounds



17. If 35% of a company's advertising budget is \$7,000, what is the full advertising budget? Show your work.

\$

bottles

liters

%

- **18.** A rectangle has a base of 4 feet and a height of 18 inches. The area of the rectangle is:
 - A 34 square inches. C 6 square feet
 - (B) 72 square inches (D) 4.5 square feet.
- **19.** An empty bottle of olive oil has a capacity of 750 mL. How many empty bottles could be filled with 4.5 L of olive oil? Show your work.
- 20. In a lab, Chemical A and Chemical B are mixed in a ratio of 2 to 3.

Part A

How much of Chemical B is needed to mix with 18 liters of Chemical A? Explain your answer.

Part B

What percent of the mixture is Chemical A? Explain your answer.

Part C

If the ratio of Chemical A to Chemical B was 4 to 5, would Chemical A be a greater or a lesser percent of the mixture? Explain your answer.



21. On Friday, Pizza Place sold a total of 120 pizzas.

Part A

30% of the pizzas sold were plain cheese pizzas. How many plain cheese pizzas were sold? Show or explain how you got your answer.

plain cheese pizzas were sold

Part B

Thirty of the pizzas sold were vegetarian pizzas. What percent of the pizzas sold were vegetarian pizzas? Show or explain how you got your answer.

Part C

On Saturday, Pizza Place again sold 30 vegetarian pizzas, which was 10% of the total number of pizzas sold on that day. What was the total number of pizzas sold on Saturday? Show or explain how you got your answer.

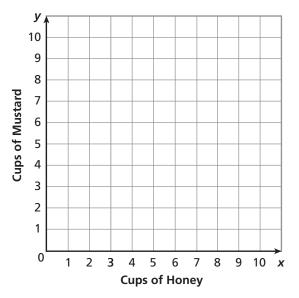
%



22. Arun's honey-mustard sauce has 3 cups honey and 4 cups mustard. Ben's honey-mustard sauce has 5 cups honey and 8 cups mustard.

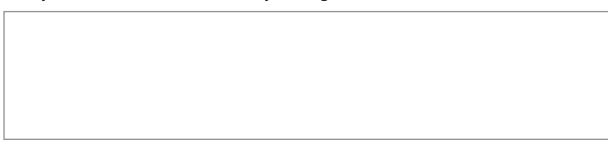
Part A

Graph and label a line to represent each ratio.



Part B

Explain how to use the two lines and a straightedge to determine whose honey-mustard sauce is more honey-tasting.



Part C

Jenna makes a sauce with 4 cups of honey and 6 cups of mustard. Order the three sauces from most to least honey-tasting. Explain your reasoning.